

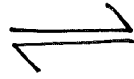
Grasping

Outline for the next many lectures:

MANIPULATION PLANNING

ARM PLANNING

Producing collision-free motions
of arm and hand



GRASP PLANNING

Producing a stable grasp of
the object.

Heavily Interconnected.

Can't grasp something unless the arm can get there.
Arm needs to know where to go.

Next few lectures / and HW!

GRASP PLANNING

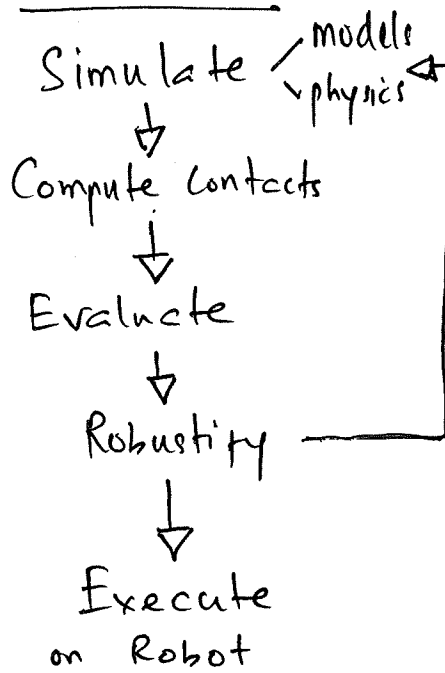


Today's lecture

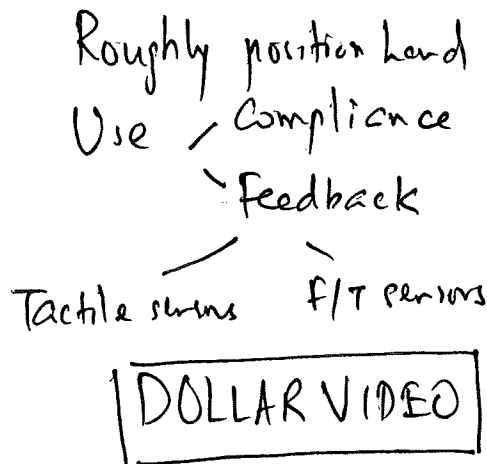
VERIFICATION: Given a grasp of an object by a hand,
is it STABLE?

GRASPING PHILOSOPHY

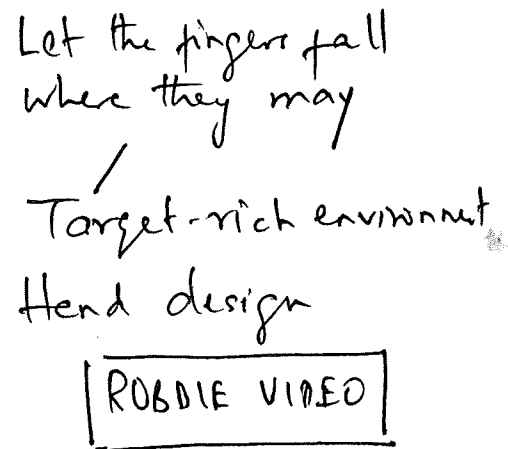
PLANNING



REACTIVE



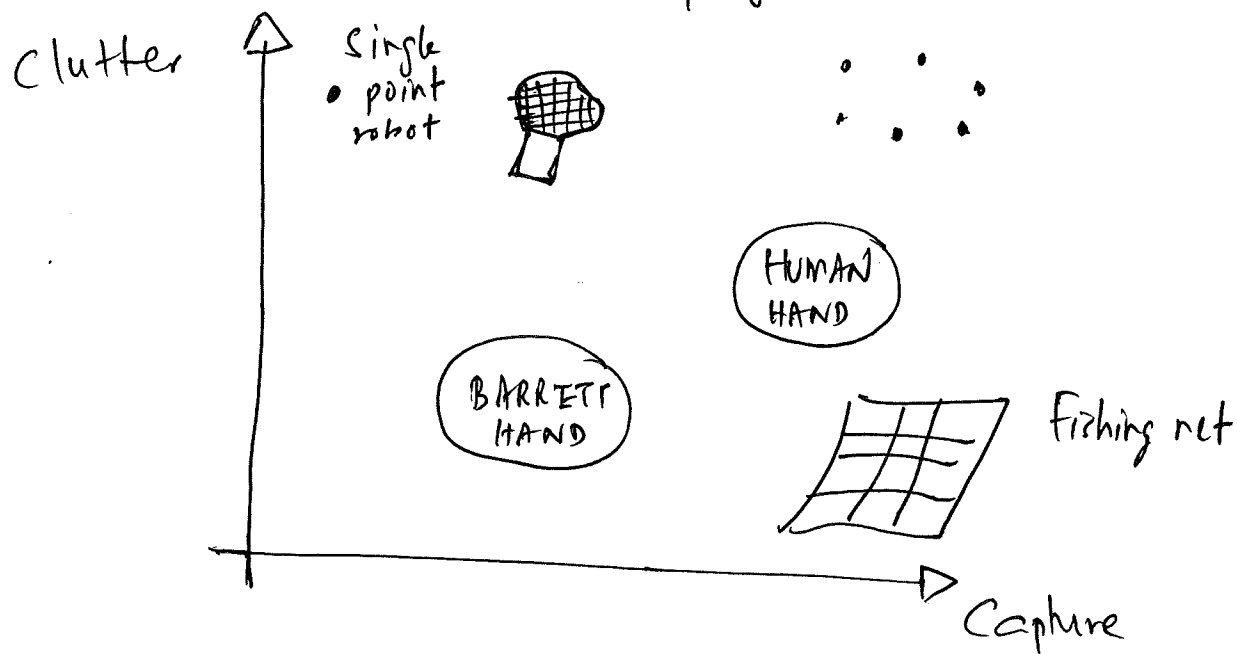
OPPORTUNISTIC



← HUMAN STRATEGY? →

HAND DESIGN

Does more DOFs ~~mean~~ imply greater GENERALITY?

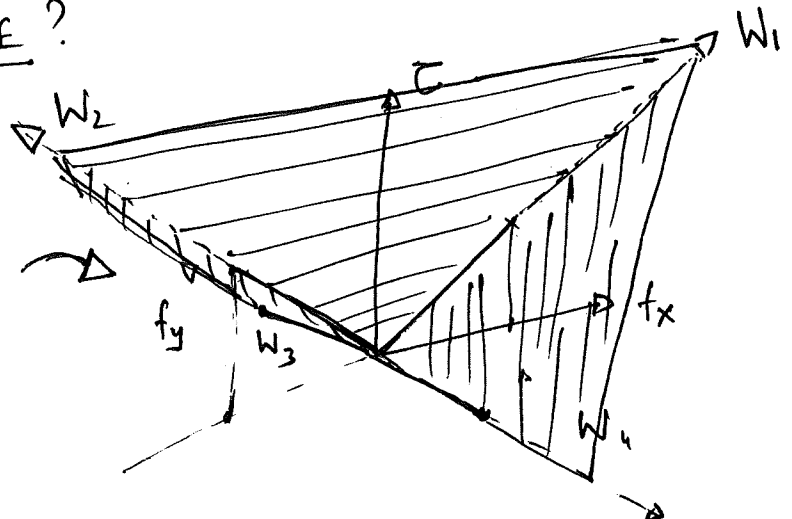
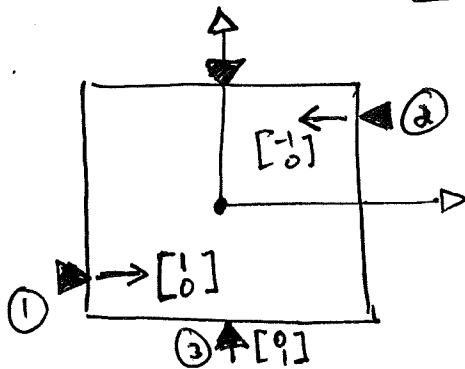


GRASP VERIFICATION

Given: ① Object Geometry

② Contact points and normals on the object.

IS THE GRASP STABLE?



Assume frictionless point contact

$$\hat{n}_1 = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$\hat{n}_2 = \begin{bmatrix} -1 \\ 0 \end{bmatrix}$$

$$\hat{n}_3 = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$\hat{n}_4 = \begin{bmatrix} 0 \\ -1 \end{bmatrix}$$

$$\vec{r}_1 = \begin{bmatrix} -1 \\ -1 \end{bmatrix}$$

$$\vec{r}_2 = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$\vec{r}_3 = \begin{bmatrix} 0 \\ -1 \end{bmatrix}$$

$$\vec{r}_4 = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$W_1 = \begin{bmatrix} \hat{n}_1 \\ \vec{r}_1 \times \hat{n}_1 \end{bmatrix}$$

$$W_2 = \begin{bmatrix} \hat{n}_2 \\ \vec{r}_2 \times \hat{n}_2 \end{bmatrix}$$

$$W_3 = \begin{bmatrix} \hat{n}_3 \\ \vec{r}_3 \times \hat{n}_3 \end{bmatrix}$$

$$W_4 = \begin{bmatrix} \hat{n}_4 \\ \vec{r}_4 \times \hat{n}_4 \end{bmatrix}$$

$$= \begin{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} \begin{bmatrix} -1 \\ 0 \end{bmatrix} \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

$$= \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix}$$

$$W_1 = W_1 f_1 \quad f_1 \geq 0$$

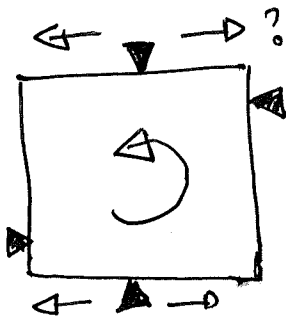
$$W_2 = W_2 f_2 \quad f_2 \geq 0$$

$$W_3 = W_3 f_3 \quad f_3 \geq 0$$

$$W_4 = W_4 f_4 \quad f_4 \geq 0$$

UNILATERAL CONTACT

ARE WE DONE?



CANNOT RESIST A
UNIT + TORQUE

SIDEBAR : Force Closure

Instantaneous

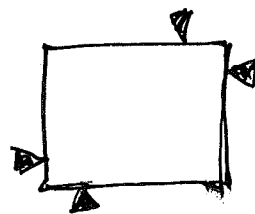
vs Form Closure.

Non-instantaneous.

~~Allowable motion of object~~
Only non-penetrating in its next configuration of object is its current configuration.

Should the contacts move to the left or to the right?

Answer: LEFT does not resist torque.
RIGHT does!



Force closure = The ability to resist an arbitrary wrench.

$$W = [W_1 f_1 + W_2 f_2 + W_3 f_3 + W_4 f_4] = \begin{bmatrix} | & | & | & | \\ W_1 & W_2 & W_3 & W_4 \\ | & | & | & | \end{bmatrix} \begin{bmatrix} f_1 \\ f_2 \\ f_3 \\ f_4 \end{bmatrix}$$

G : Grasp Map

$$= \begin{matrix} \cancel{G} f \\ \swarrow \searrow \\ 3 \times 4 \quad 4 \times 1 \end{matrix}$$

$$\forall W_{ext}, \exists f \geq 0 : Gf = W_{ext}$$

Constructive check

① $Gf, f > 0$ must span \mathbb{R}^3 or \mathbb{R}^6

➔ ② Origin 0 lies completely inside the unit wrench polyhedron.

INTUITION: $Gf = 0, f > 0$ is INTERNAL FORCE.

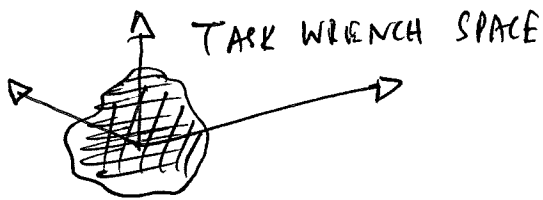
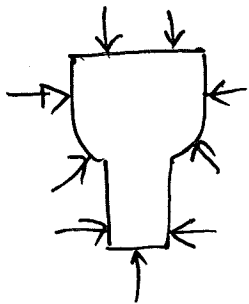
GRASP QUALITY METRICS.

① Radius of largest inscribed ball. \uparrow

② Volume of GWS $\propto \sqrt{\det(GGT)}$ \uparrow

ISSUES

Very conservative. Blind to task.

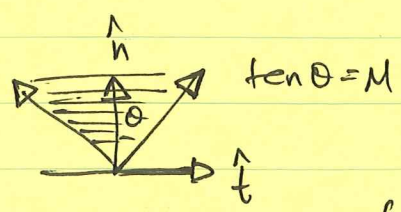


① Radius of largest TWS \uparrow

② $\frac{\text{Vol. TWS}}{\text{Vol. GWS}}$ \downarrow

WHAT HAPPENS WITH FRICTION?

IN 2D

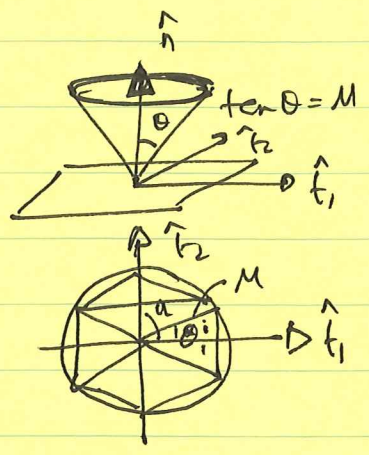


$$f = \begin{bmatrix} f_L & f_R \end{bmatrix} \begin{bmatrix} \alpha_1 \\ \alpha_2 \end{bmatrix}$$

$\alpha_1, \alpha_2 \geq 0$

$$f_L = \begin{bmatrix} \mu & -\mu \\ 1 & 1 \end{bmatrix}$$

IN 3D

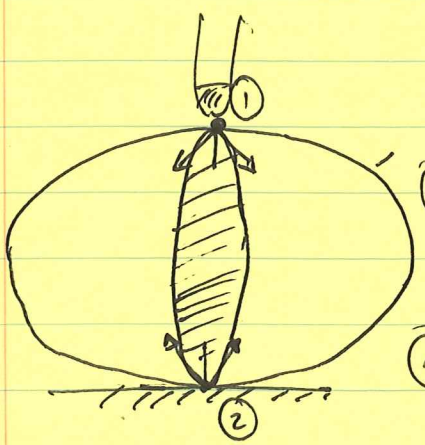


$$f = \begin{bmatrix} f_1 & f_2 & \dots & f_k \end{bmatrix} \begin{bmatrix} \alpha_1 \\ \alpha_2 \\ \vdots \\ \alpha_k \end{bmatrix}$$

$$= \begin{bmatrix} \mu \cos \theta_1 & & & \mu \cos \theta_k \\ \mu \sin \theta_1 & \dots & & \mu \sin \theta_k \\ 1 & & & 1 \end{bmatrix} \begin{bmatrix} \alpha_1 \\ \alpha_2 \\ \vdots \\ \alpha_k \end{bmatrix}$$

Polyhedral approximation.

ISSUES



- ① Which one is more stable?
Uncertainty.
- ② ~~Object~~ How do we get to contacts?
Dynamics.